

Polynomials Review Assignment

1. Fill in the following information for each polynomial.

	$3 - a^2 + 2a^2b$	$x^2y - y^2 + 4y$	$a^2b - b$	$3s^4t^3$
Coefficients:	-1, 2	1, -1, 4	1, -1	3
Variables:	a, b	x, y	a, b	s, t
# of Terms:	3	3	2	1
Name:	trinomial	trinomial	binomial	monomial
Degree of Each Term:	n/a, 2, 3	3, 2, 1	3, 1	7
Degree of Polynomial:	3	3	3	7

2. Which expression represents the result of simplifying $(4x - 1) - (x + 1)$? (multiple choice)

A) $5x + 2$

B) $3x - 2$

C) $5x$

D) $3x$

$$\begin{aligned}
 &= 4x - 1 - x - 1 \\
 &= 4x - x - 1 - 1 \\
 &= 3x - 2
 \end{aligned}$$

3. Remove brackets and collect like terms. Then, simplify.

a) $(x+3) + (x+5)$

$= x + 3 + x + 5$

$= x + x + 3 + 5$

$= 2x + 8$

b) $(2y-5) + (y+9)$

$= 2y - 5 + y + 9$

$= 2y + y - 5 + 9$

$= 3y + 4$

c) $(3v-2) + (6-v)$

$= 3v - 2 + 6 - v$

$= 3v - v - 2 + 6$

$= 2v + 4$

d) $(k+4) + (2-3k) + (6k-1)$

$= k + 4 + 2 - 3k + 6k - 1$

$= k - 3k + 6k + 4 + 2 - 1$

$= 4k + 5$

4. Simplify

$$\begin{aligned} \text{a)} \quad & (6k-4) + (2k+4) \\ & = 6k - 4 + 2k + 4 \\ & = 6k + 2k - \cancel{4} + \cancel{4} \\ & = 8k \end{aligned}$$

$$\begin{aligned} \text{b)} \quad & (b-6) - (2-5b) + (b+4) \\ & = b - 6 - 2 + 5b + b + 4 \\ & = b + 5b + b - 6 - 2 + 4 \\ & = 7b - 4 \end{aligned}$$

$$\begin{aligned} \text{c)} \quad & (x+2) - (1-x) - (5+x) \\ & = x + 2 - 1 + x - 5 - x \\ & = x + \cancel{x} - \cancel{x} + 2 - 1 - 5 \\ & = x - 4 \end{aligned}$$

$$\begin{aligned} \text{d)} \quad & (g+12) + (g-7) - (2-3g) \\ & = g + 12 + g - 7 - 2 + 3g \\ & = g + g + 3g + 12 - 7 - 2 \\ & = 5g + 3 \end{aligned}$$

$$\begin{aligned} \text{e)} \quad & (1-b) + (3+2b) - (b-8) \\ & = 1 - b + 3 + 2b - b + 8 \\ & = -b + 2b - b + 1 + 3 + 8 \\ & = -\cancel{2b} + \cancel{2b} + 12 \\ & = 12 \end{aligned}$$

$$\begin{aligned} \text{f)} \quad & (x^2 + 2x + 1) + (2x^2 + 4) \\ & = x^2 + 2x + 1 + 2x^2 + 4 \\ & = x^2 + 2x^2 + 2x + 1 + 4 \\ & = 3x^2 + 2x + 5 \end{aligned}$$

5. Simplify the following to a single power. Then evaluate.

$$\begin{aligned}
 \text{a) } & \left(-\frac{3}{7}\right)^6 \div \left(-\frac{3}{7}\right)^3 \\
 & \quad \uparrow \quad \quad \uparrow \\
 & \quad \text{same base} \\
 & = \left(-\frac{3}{7}\right)^{6-3} \\
 & = \left(-\frac{3}{7}\right)^3 \\
 & = \frac{-3^3}{7^3} \\
 & = \frac{-27}{343}
 \end{aligned}$$

$$\begin{aligned}
 \text{b) } & \frac{0.2^4 \times 0.2^3 \div 0.2^2}{(0.2^2)^2} \\
 & = \frac{0.2^{4+3-2}}{0.2^{2 \times 2}} \\
 & = \frac{0.2^5}{0.2^4} \\
 & = 0.2^{5-4} \\
 & = 0.2^1 \\
 & = 0.2
 \end{aligned}$$

6. Simplify using the exponent laws, then evaluate the expression.

$$\begin{aligned}
 \text{a) } & \left[\left(\frac{1}{3}\right)^3\right]^3 \\
 & = \left(\frac{1}{3}\right)^{3 \times 3} \\
 & = \left(\frac{1}{3}\right)^9 \\
 & = \frac{1^9}{3^9} \\
 & = \frac{1}{19683}
 \end{aligned}$$

$$\begin{aligned}
 \text{b) } & [(-3)^4]^2 \times (-3)^5 \div [(-3)^2]^5 \\
 & = (-3)^{4 \times 2} \cdot (-3)^5 \div (-3)^{2 \times 5} \\
 & = (-3)^8 \cdot (-3)^5 \div (-3)^{10} \\
 & = (-3)^{8+5-10} \\
 & = (-3)^3 \\
 & = -27
 \end{aligned}$$

7. Simplify.

$$\begin{aligned}
 \text{a) } & (-x^3)^5 (4x^2)^2 \\
 & = [-x^{3 \cdot 5}] [4^2 x^{2 \cdot 2}] \\
 & = (-x^{15}) (16x^4) \\
 & = -16x^{15+4} \\
 & = -16x^{19}
 \end{aligned}$$

$$\begin{aligned}
 \text{b) } & \frac{10g^4h^5 \times (3g^3h^2)^2}{(4h^2)^2 \times 3g^3h^2} \quad \text{*challenge question} \\
 & = \frac{10g^4h^5 \cdot 3^2 g^{3 \times 2} h^{2 \times 2}}{4^2 g^{1 \times 2} h^{2 \times 2} \cdot 3g^3h^2} \\
 & = \frac{10g^4h^5 \cdot 9g^6h^4}{16g^2h^4 \cdot 3g^3h^2} \\
 & = \frac{(10 \times 9) g^{4+6} h^{5+4}}{(16 \times 3) g^{2+3} h^{4+2}} \\
 & = \frac{90 g^{10} h^9}{48 g^5 h^6} \\
 & = \frac{15}{8} g^{10-5} h^{9-6} \\
 & = \frac{15}{8} g^5 h^3
 \end{aligned}$$

8. Expand by distribution.

$$\begin{aligned} \text{a) } & 3(g+4) \\ & = 3g+12 \end{aligned}$$

$$\begin{aligned} \text{b) } & -4(-w-5) \\ & = 4w+20 \end{aligned}$$

$$\begin{aligned} \text{c) } & r(3r+5) \\ & = 3r^2+5r \end{aligned}$$

$$\begin{aligned} \text{d) } & w(4w-5) \\ & = 4w^2-5w \end{aligned}$$

$$\begin{aligned} \text{e) } & (2q+5)(6) \\ & = 12q+30 \end{aligned}$$

$$\begin{aligned} \text{h) } & (6w-4)(-3w) \\ & = -18w^2+12w \end{aligned}$$

9. Expand and simplify

$$\begin{aligned} \text{a) } & 2(b+3) + 5(b+4) \\ & = 2b+6 + 5b+20 \\ & = 2b+5b+6+20 \\ & = 7b+26 \end{aligned}$$

$$\begin{aligned} \text{b) } & -(d-4) - 4(d+2) \\ & = -d+4 - 4d-8 \\ & = -d-4d+4-8 \\ & = -5d-4 \end{aligned}$$

$$\begin{aligned} \text{c) } & 5[4s - (s+2)] & \text{d) } & 3[-2(6-t) + 5t] \\ & = 5[4s - s - 2] & & = 3[-12 + 2t + 5t] \\ & = 5[3s - 2] & & = 3[-12 + 7t] \\ & = 15s - 10 & & = -36 + 21t \\ & & & = 21t - 36 \end{aligned}$$

10. Simplify the following expressions.

$$\begin{aligned} \text{a) } & 3(3x^2 - 2x - 1) \\ & = 9x^2 - 6x - 3 \end{aligned}$$

$$\begin{aligned} \text{b) } & 2a(5a - 6) \\ & = 10a^2 - 12a \end{aligned}$$

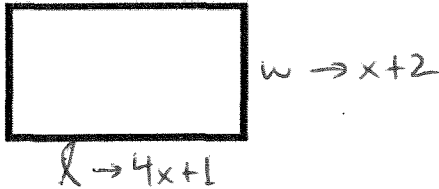
$$\begin{aligned} \text{c) } & 4 + 6(2x - 3) \\ & = 4 + 12x - 18 \\ & = 12x - 18 + 4 \\ & = 12x - 14 \end{aligned}$$

$$\begin{aligned} \text{d) } & -5x - 3x(2x+5) + x(6x+2) \\ & = -5x - 6x^2 - 15x + 6x^2 + 2x \\ & = \cancel{-6x^2} + \cancel{6x^2} - 5x - 15x + 2x \\ & = -18x \end{aligned}$$

$$\begin{aligned} \text{e) } & 1 + a(3a-3) - 4a + 2a(2a-1) \\ & = 1 + 3a^2 - 3a - 4a + 4a^2 - 2a \\ & = 3a^2 + 4a^2 - 3a - 4a - 2a + 1 \\ & = 7a^2 - 9a + 1 \end{aligned}$$

11. A rectangle has length $4x + 1$ and width $x + 2$.

a) Label the diagram.



b) Write a simplified expression for the perimeter of the rectangle.

$$P = 2(l + w)$$

$$P = 2(4x + 1 + x + 2)$$

$$P = 2(5x + 3)$$

$$P = 10x + 6$$

c) Find the perimeter of the rectangle when $x = 5$.

$$P = 10x + 6 \quad \boxed{x = 5}$$

$$P = 10(5) + 6$$

$$P = 50 + 6$$

$$P = 56$$

\therefore The perimeter is 56 (no units specified)

12. Three artists contributed to a coffee-table book. They each chose to be paid a different way.

Artist	Fixed Rate (\$)	Royalty (\$ per n books sold)	
Ayesha	1000	$2n$	$\rightarrow 1000 + 2n = E$
Jorge	-	$5n$	$\rightarrow 5n = E$
Ioana	4000	-	$\rightarrow 4000 = E$

a) Write an expression for the total earnings for each artist.

b) Write a simplified expression for the total amount paid to Ayesha, Jorge, and Ioana.

$E =$ add all 3 together

$$E = (1000 + 2n) + (5n) + (4000)$$

$$E = 1000 + 4000 + 2n + 5n$$

$$E = 7n + 5000$$

13. Consider the following composite figure.
a) Find a simplified expression for the area.

Area shape #1 Area shape #2

$$A = l \cdot w$$

$$A = x \cdot (2x - 1)$$

$$A = 2x^2 - x$$

Add up

$$A = 2x^2 - x + 3x^2$$

$$A = 5x^2 - x$$

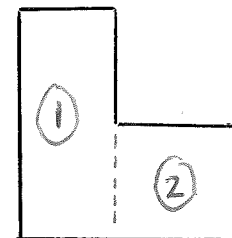
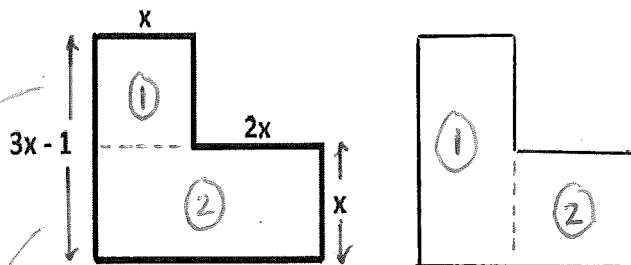
b) Find a simplified expression for the perimeter.

P = Add up all the sides

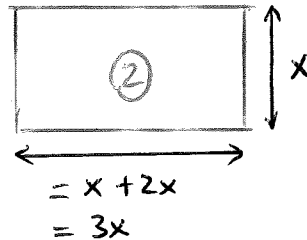
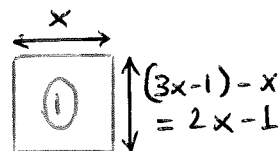
$$P = (3x - 1) + x + (2x - 1) + 2x + x + 3x$$

$$P = 3x + x + 2x + 2x + x + 3x - 1 - 1$$

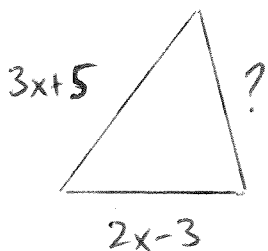
$$P = 12x - 2$$



choose either method but split into 2 pieces



14. A triangle has a perimeter of $9x + 12$. If two of its sides have lengths of $3x + 5$ and $2x - 3$, find the missing side.



$$P = 9x + 12$$

$$P = (3x + 5) + (2x - 3) + ?$$

$$9x + 12 = 3x + 5 + 2x - 3 + ?$$

$$9x + 12 = 3x + 2x + 5 - 3 + ?$$

$$9x + 12 = 5x + 2 + ?$$

$$9x - 5x + 12 - 2 = ?$$

$$4x + 10 = ?$$