Introduction: Word Problems

Match each sentence with the correct equation (place the question number beside the answer):

1. A number **increased by** three **is equal** to nine. $x - 9 = 6$

   _____

2. A number **decreased by** four **is equal** to twelve. $\frac{x}{3} = 8$

   _____

3. Four **times** a number **is equal** to sixteen. $x + 3 = 9$

   _____

4. A number **divided by** three **is** eight. $2x + 3y = 27$

   _____

5. John's age will be nineteen in three years. $x - 4 = 12$

   _____

6. Nine years **ago**, Mary's age was six. $x^2 = 16$

   _____

7. Six **less** than a number is 10. $0.05x + 0.25y = 5.65$

   _____

8. A number **increased by** five **is equal** to negative four. $4x = 16$

   _____

9. The **square** of a number **is** sixteen. $x - 6 = 10$

   _____

10. A number **divided by** six **is equal** to three. $x + 3 = 19$

    _____

11. I have x nickels and y quarters. I have **a total of** $5.65 $\frac{x}{6} = 3$

    _____

12. It takes 2 hours to mow a lawn and 3 hours to weed a $x + 5 = -4$
garden. In one month I mowed x lawns and weeded y   _____
gardens. It took 27 hours.

**In word problems, first we change language statements into
mathematical statements (equations) and then solve for the variable.**

Complete: CP # 30, 31 and 32   Page 1

1. Use the first clue to create a LET statement which shows how the variable represents the unknown quantities in the problem.

2. Write the second unknown in terms of the first. HINT: The second unknown is compared to the first unknown.

3. Create an equation from the second clue. Do NOT include units in equations.

4. Solve the equation.

5. Use the answer to #4 to determine the value of the other unknowns found in the LET statements.

6. Conclusion: Answer the question in sentence form – include units.

Example: Jenna ran 5 kilometres more than Kelly. The two girls ran a total of 27 kilometres. How far did each of them run?

Solution:

Number Questions

1. a) A certain number is twice another number. What are the possible values for the sum of these two numbers?

First Number	1	2	3	7	9	100	*n*
Second Number							
Sum							

   b) One number is increased by 6 to get a second number. In terms of n, how can we represent:

   The first number?_____   The second number? _____   The sum? _____

   c) One number is decreased by 3 to get a second number. In terms of n, how can we represent:

   The first number?_____   The second number? _____   The sum? _____

   d) The second number is four less than seven times the first number. In terms of n, how can we represent:

   The first number?_____   The second number? _____   The sum? _____

   e) The second number is three more than one-half the first number. In terms of n, how can we represent:

   The first number?_____   The second number? _____   The sum? _____

Applying to Problems

2. a) One number is three times another number. If the sum of the numbers is 36, determine the two numbers.

b) One number is four more than twice another number. If both numbers are positive and the difference between the numbers is 27, determine the numbers.

c) Brian ran 2 km less than Tom. They ran a total distance of 12 km. Find how far each ran.

In your notebooks, give full solutions to the following problems.

3. a) Lake Ontario is 4 times as deep as Lake Erie. The sum of their depths is 300 metres. What is the depth of each lake?
    b) Angel waterfall in Venezuela is 20 times as high as Niagara Falls. The difference between their heights is 950 metres. What is the height of each of the falls?
    c) Lake Erie is 77 kilometres longer than Lake Ontario. Their length total 697 kilometres. Find the length of each lake.
    d) Lacey is three times as old as Joey. The difference in their ages is 12 years. Find their ages.
    e) Bill's mother is 22 years older than he is. The sum of their ages is 60. Find their ages.
    f) One number is 5 more than another number. Three times the greater plus twice the lesser is 30. Determine the numbers.